

Telecom Network Systems

Friis Deep Space Com

$$\begin{aligned}
 1) \quad 6 \text{ Gb/s (SATA 3)} &= 6 \cdot 10^9 \text{ b/s} \\
 1 \text{ bit} &= \ln(2) \cdot kT = \frac{2.57 \cdot 10^{-21} \text{ J/b}}{\times} \\
 &= 1.7 \cdot 10^{-11} \text{ W}
 \end{aligned}$$

- 2) A 'point' antenna, or 'isotropic' antenna has a power-conversion efficiency that is depending on wavelength^{*}. The power of^{output} the antenna that is placed in a radiation field with density (W/m²) given by S , is given by

$$P_{R,iso} = S \cdot \frac{\lambda^2}{4\pi}$$

A real antenna has

$$P_{R,real} = S \cdot A_R$$

This defines an efficiency of receiving antenna

$$G_R \equiv \frac{P_{R,real}}{P_{R,iso}} = \frac{4\pi A_R}{\lambda^2}$$

* : See Wikipedia Free space path loss

(2)

or

$$P_{R, \text{real}} = P_{R, \text{iso}} \cdot G_R$$

$$= S \cdot \frac{\lambda^2}{4\pi} \cdot G_R$$

On the other side, the transmitting antenna also has an efficiency G_T . That means that the receiving antenna, at distance L sits in a power density

$$S = \frac{P_T \cdot G_T}{4\pi L^2} \begin{matrix} \nearrow \frac{4\pi A_T}{\lambda^2} \\ \searrow \text{distance effect} \\ \text{(sphere surface)} \end{matrix}$$

Then

$$P_{R, \text{real}} = S \cdot \frac{\lambda^2}{4\pi} G_R$$

$$= \frac{P_T G_T}{4\pi L^2} \cdot \frac{\lambda^2}{4\pi} G_R$$

$$= \frac{P_T}{4\pi L^2} \cdot \frac{4\pi A_T}{\lambda^2} \cdot \frac{\lambda^2}{4\pi} \cdot \frac{4\pi A_R}{\lambda^2}$$

$$= \frac{P_T A_R A_T}{\lambda^2 L^2}$$

q.e.d.

(3)

$$3) P_T = 10 \text{ W}$$

$$A_T = 10 \text{ m}^2$$

$$A_R = 1000 \text{ m}^2$$

$$\lambda = 1 \text{ cm}$$

$$L = 5 \cdot 10^{12} \text{ m}$$

$$P_R = \frac{P_T \cdot A_R \cdot A_T}{\lambda^2 L^2}$$

$$= 4 \cdot 10^{-17} \text{ W}$$

$$T = 4 \text{ K} \Rightarrow \ln(2) kT = 3.83 \cdot 10^{-23} \text{ J/bit}$$

$$P_R / E_{\text{bit}} = 4 \cdot 10^{-17} \frac{\text{J}}{\text{s}} / 3.83 \cdot 10^{-23} \text{ J/bit}$$

$$= 1.04 \text{ Mb/s}$$

$$4) P_T = 10 \text{ W}$$

$$A_T = 1 \text{ m}^2$$

$$A_R = 100 \text{ m}^2$$

$$\lambda = 6 \cdot 10^{-7} \text{ m}$$

$$L = 5 \cdot 10^{12} \text{ m}$$

$$P_R = \frac{P_T A_R A_T}{\lambda^2 L^2} = 1.11 \cdot 10^{-10} \text{ W}$$

$$T = 350 \text{ K} \Rightarrow \ln(2) kT = 2.87 \cdot 10^{-21} \text{ J/bit}$$

$$P_R / E_{\text{bit}} = 1.11 \cdot 10^{-10} \frac{\text{J}}{\text{s}} / 2.87 \cdot 10^{-21} \frac{\text{J}}{\text{bit}}$$

$$= 39 \text{ Gb/s}$$

5) $P = 1.11 \cdot 10^{-10} \text{ W}$

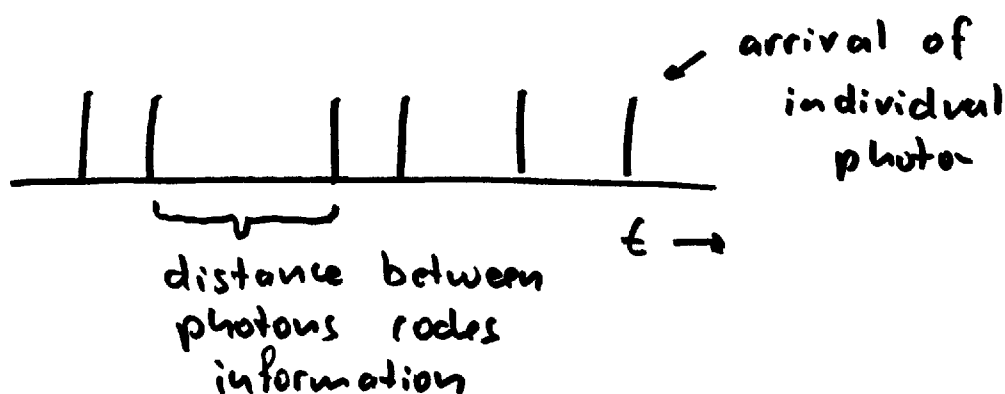
(4)

$$E_{\text{phot}} = h\nu = \frac{hc}{\lambda} = 3.31 \cdot 10^{-19} \text{ J}$$

$$\text{flux} = \frac{P}{E_{\text{phot}}} = 3.36 \cdot 10^8 \text{ photons/s}$$

$$\text{bits/photon} = \frac{3.9 \cdot 10^9 / \text{s}}{3.36 \cdot 10^8 \text{ phot/s.}} = 116 \text{ bits/photon}$$

$\Rightarrow$ with time modulation we can have any number of bits per photon



$$6) I(\nu, T) = \frac{2h\nu^3}{c^2} \cdot \frac{1}{\exp(\frac{h\nu}{kT}) - 1}$$

See <http://physics.info/planck/>

Note: Wien already did the work

for us: $\lambda_{\text{max}} = \frac{b}{T}$

b is Wien's constant = $2.898 \cdot 10^{-3} \text{ mK}$

$T = 5800 \Rightarrow \lambda_{\text{max}} = 500 \text{ nm}$